



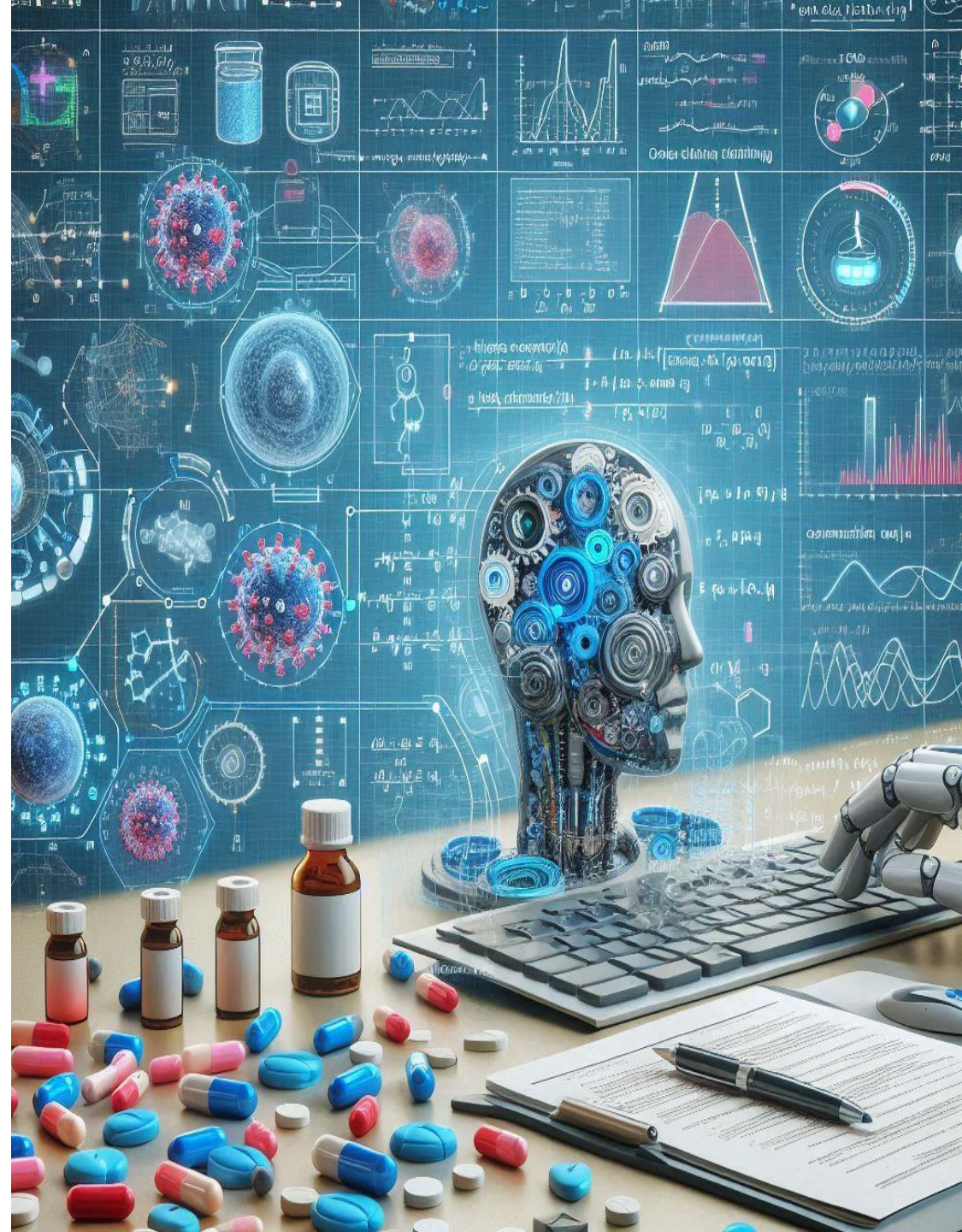
Machine learning for pharmacometrics: examples of applications

Destere Alexandre,

PharmD, PhD

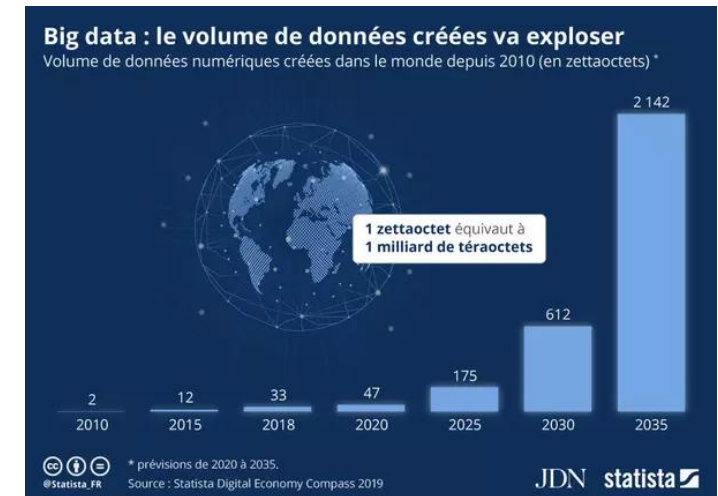
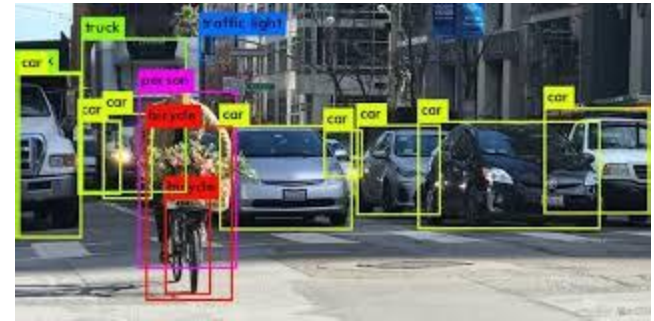
Department of Clinical Pharmacology – university Hospital of Nice

Maasai Team – Inria/3IA – Université Côte d'Azur



Introduction to machine learning

- Machine learning (ML) is widely used in different aspects of our lives
 - Image recognition¹
 - Text generation (ChatGPT or Gemini)
 - Big data analysis
 - Quantitative structure-activity relationship (QSAR)²
 - Discovery of a new antibiotic³
 - Alpha fold DeepMind⁴
 - Increase of data availability
 - Computational power + dedicated packages (R & Python)



¹ Shen, D., Wu, G. & Suk, H.-I. Deep Learning in Medical Image Analysis. *Annu. Rev. Biomed. Eng.* **19**, 221–248 (2017).

² Chan, H. C. S., Shan, H., Dahoun, T., Vogel, H. & Yuan, S. Advancing Drug Discovery via Artificial Intelligence. *Trends Pharmacol. Sci.* **40**, 592–604 (2019)

³ Stokes, J. M. et al. A Deep Learning Approach to Antibiotic Discovery. *Cell* **180**, 688–702.e13 (2020)

⁴ Jumper et al Highly accurate protein structure prediction with AlphaFold *Nature* 583–589 (2021)

Introduction to machine learning



← Tweet

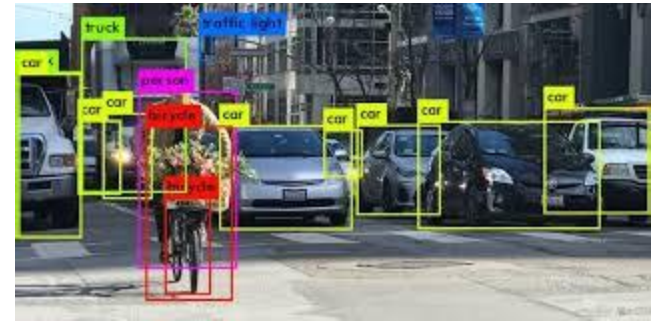


François Chollet ✓
@fchollet

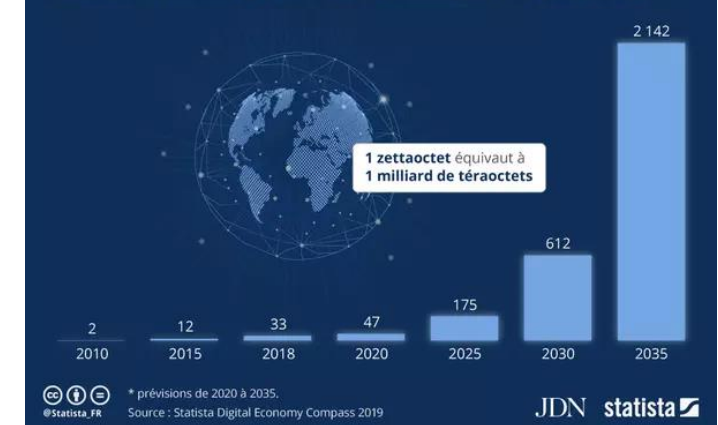
With tools like Colab, Keras, and TensorFlow, virtually anyone can solve in a day, with no initial investment, problems that would have required an engineering team working for a quarter and \$20k in hardware in 2014

[Traduire le Tweet](#)

10:03 PM · 20 nov. 2020 · Twitter for Android



Big data : le volume de données créées va exploser
Volume de données numériques créées dans le monde depuis 2010 (en zettaoctets) *



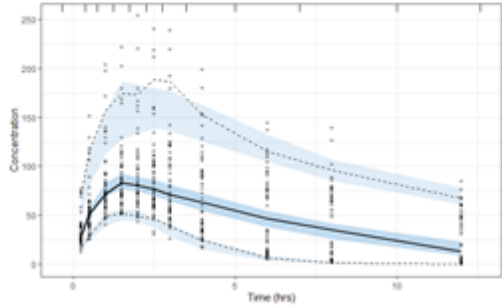
¹ Shen, D., Wu, G. & Suk, H.-I. Deep Learning in Medical Image Analysis. *Annu. Rev. Biomed. Eng.* **19**, 221–248 (2017).

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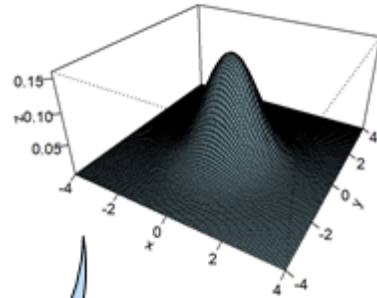
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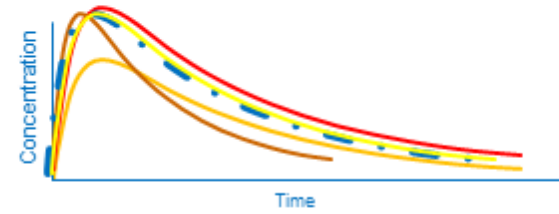
Internal model evaluation: Visual Predictive Check



No exposure information available
(i.e age, weight but no drug
measurement)
Monte Carlo Simulations (weighted
sampling in the joint distribution)

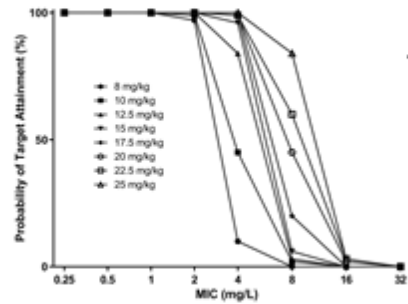


Population pharmacokinetics model



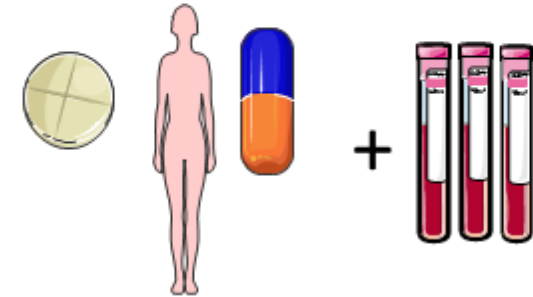
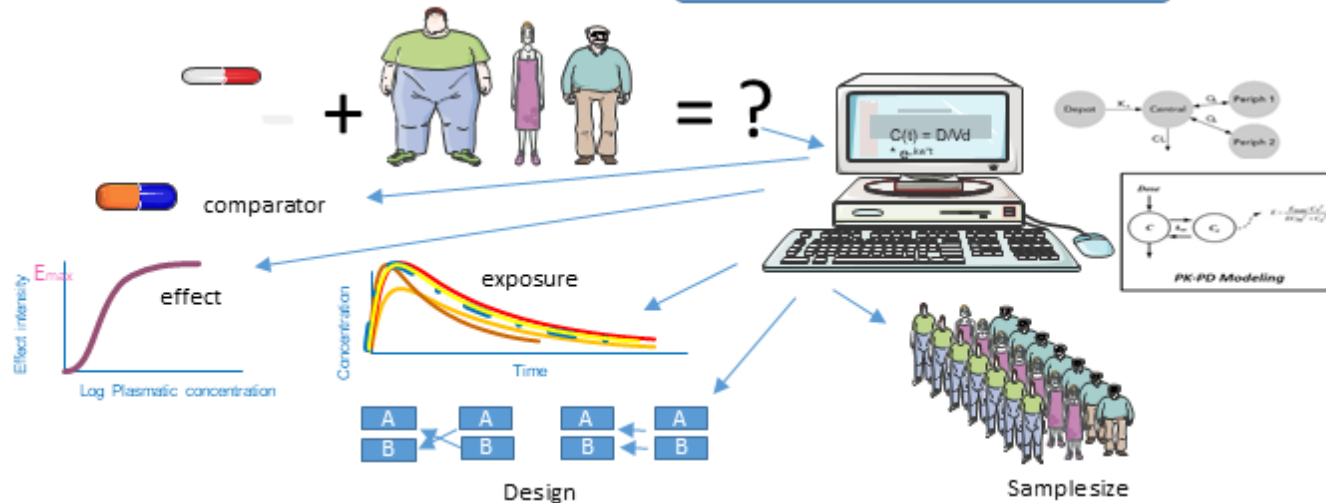
Applications of population pharmacokinetic modeling

Probability of Target Attainment



Exposure information available (ie
drug measurement) + covariable (ie
age, weight))
MAP-BE

Clinical Trial Simulations



$$P(\theta|c) = P(c|\theta) * P(\theta) / P(c)$$

Dosing recommendation (MIPD)



Comparison of standard statistics vs ML

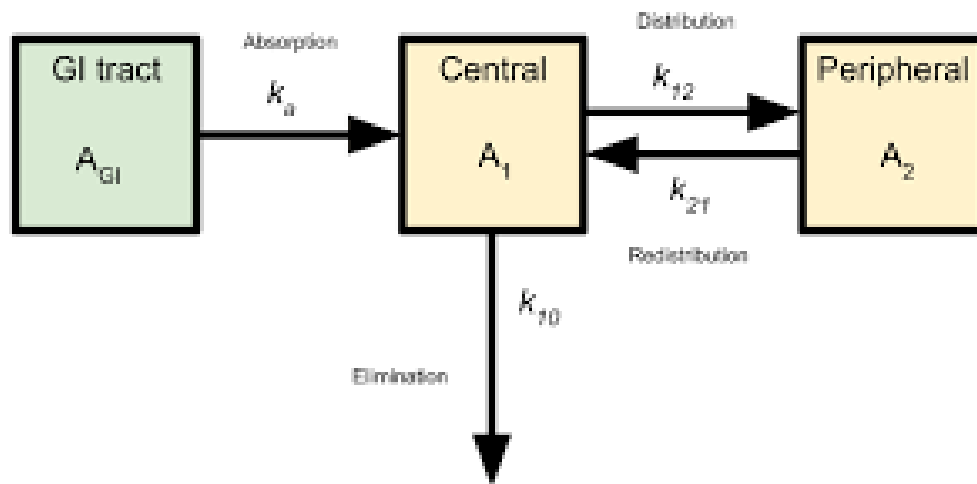
- **Standard statistical approach (POPPK):**

- Based on understanding of biological processes, interpretable
- but may be limited by current knowledge

- **Machine Learning:**

- No explicitly defined physiological model (black box)
- Complex algorithmic approach (e.g. Xgboost, neural network, SVM...)
- Large numbers of free parameters and complex interactions

→ **minimize errors between predicted and observed values (loss function)**



Comparison of standard statistics vs ML

- In simple words
 - Standard statistics: data are entered into a model to predict results
 - ML approaches, the data are fed with the results to an algorithm that constructs the model **without a priori knowledge on the underlying associations (data driven)**.
- ML methods → individual prediction
- ML methods particularly suited when there is a high degree of complexity/correlation between predictors (= “features”).

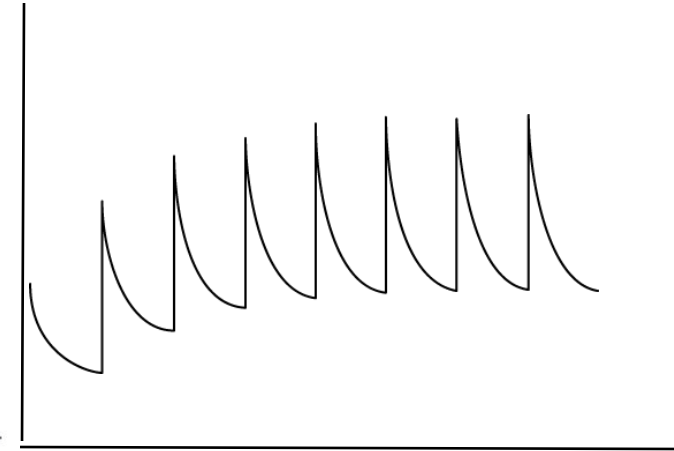
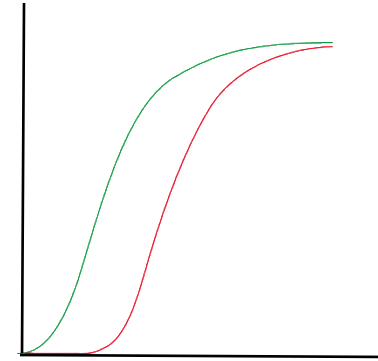


Standard statistics



Machine Learning

Use of Machine Learning in Pharmacometrics



> Clin Pharmacokinet. 2021 Feb;60(2):223-233. doi: 10.1007/s40262-020-00927-6.

A Machine Learning Approach to Estimate the Glomerular Filtration Rate in Intensive Care Unit Patients Based on Plasma Iohexol Concentrations and Covariates

Jean-Baptiste Woillard^{1 2 3}, Charlotte Salmon Gandonnière⁴, Alexandre Destere^{5 6 7},
Stephan Ehrmann^{4 8}, Hamid Merdji^{9 10}, Armelle Mathonnet¹¹, Pierre Marquet^{5 6 7},
Chantal Barin-Le Guellec^{6 12 13}

Affiliations + expand

PMID: 32794122 DOI: 10.1007/s40262-020-00927-6

> Kidney Int Rep. 2023 Nov 3;9(1):134-144. doi: 10.1016/j.ekir.2023.10.023. eCollection 2024 Jan.

Optimization of Rituximab Therapy in Adult Patients With PLA2R1-Associated Membranous Nephropathy With Artificial Intelligence

Alexandre Destere^{1 2}, Maxime Teisseyre^{3 4 5}, Diane Merino¹, Marion Cremoni^{4 6},
Alexandre O Gérard^{1 5}, Thomas Crepin⁷, Noémie Jourde-Chiche⁸, Daisy Graça^{3 4 6},
Kévin Zorzi^{3 4}, Céline Fernandez^{3 4}, Vesna Brglez^{3 4 6}, Sylvia Benzaken⁶,
Vincent L M Esnault^{3 5}, Sylvain Benito⁹, Milou-Daniel Drici¹, Barbara Seitz-Polski^{3 4 5 6}

> Pharm Res. 2022 Oct;39(10):2497-2506. doi: 10.1007/s11095-022-03351-6. Epub 2022 Aug 3.

Optimization of Vancomycin Initial Dose in Term and Preterm Neonates by Machine Learning

Laure Ponthier^{1 2}, Pauline Ensueque², Alexandre Destere^{1 3}, Pierre Marquet^{1 4},
Marc Labriffe^{1 4}, Evelyne Jacqz-Aigrain⁵, Jean-Baptiste Woillard^{6 7}

Affiliations + expand

PMID: 35918452 DOI: 10.1007/s11095-022-03351-6

Epub 2024 Mar 19.

A machine learning approach to predict daptomycin exposure from two concentrations based on Monte Carlo simulations

Cyrielle Codde¹, Florence Rivals², Alexandre Destere³, Yeleen Fromage², Marc Labriffe^{2 4},
Pierre Marquet^{2 4}, Clément Benoist⁴, Laure Ponthier⁴, Jean-François Faucher¹,
Jean-Baptiste Woillard^{2 4}

Epub 2024 Mar 16.

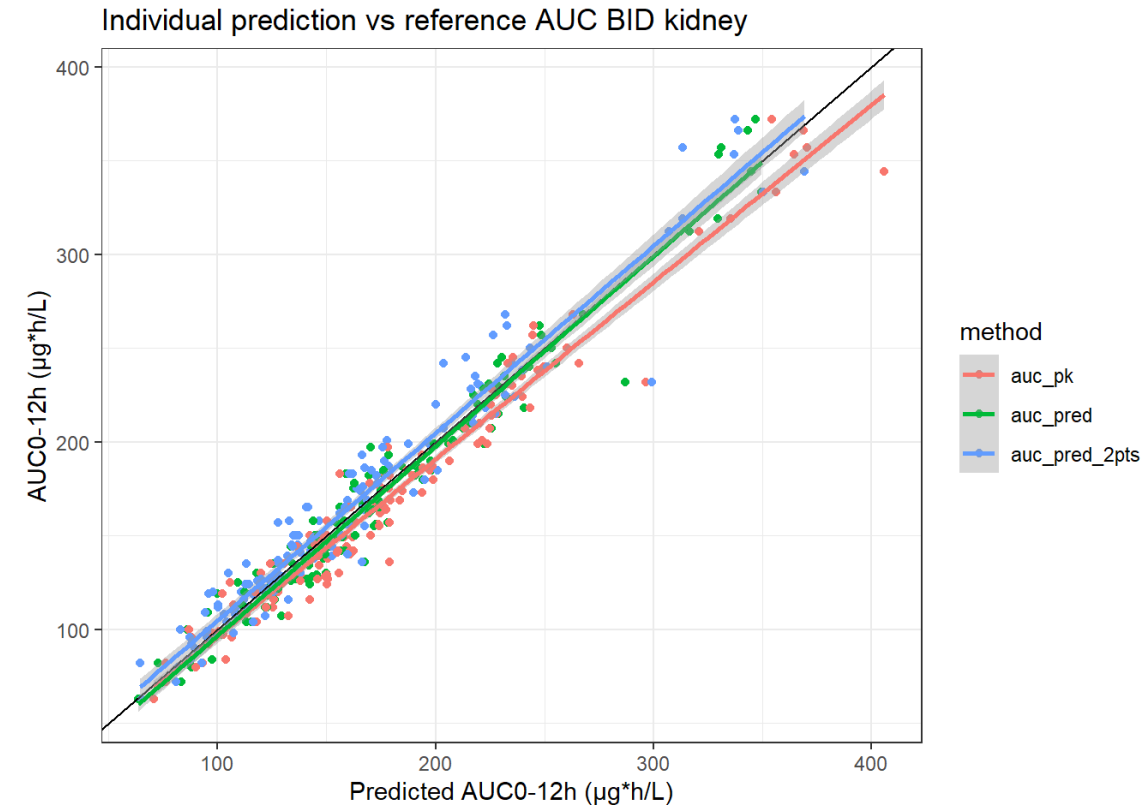
Optimization of Ganciclovir and Valganciclovir Starting Dose in Children by Machine Learning

Laure Ponthier^{1 2}, Julie Autmizguine^{3 4 5}, Benedicte Franck^{6 7}, Anders Åsberg^{8 9},
Philippe Ovetchkine⁴, Alexandre Destere¹⁰, Pierre Marquet^{1 11}, Marc Labriffe^{1 11},
Jean-Baptiste Woillard^{12 13}

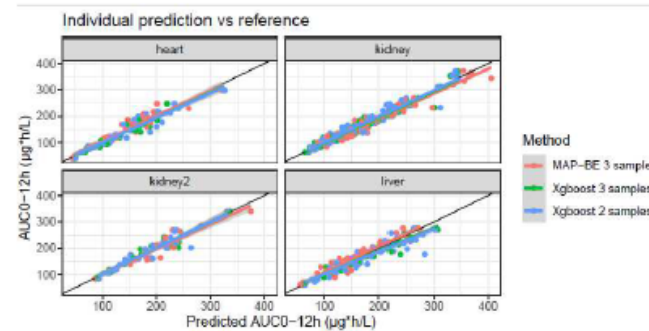
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Example: A posteriori TAC exposure

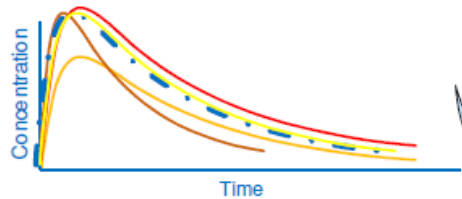
- Development of a ML model to predict the TAC AUC (TDM) based on ISBA data (<https://abis.chu-limoges.fr/login>):
3 individual concentrations / a few covariates → ~5000 AUC/~2000 patients
- Excellent performances in external full PK profiles vs ref AUC (trapezoidal) based **on 2** or 3 samples
- Bias/RMSE external data (e.g. in kidney transplant recipients) =
 - **ML** 3 samples: 2.1%/7.7%
 - **ML** 2 samples: -2.4%/8.8%
 - **POPPK** 3 samples: 5%/9.6%



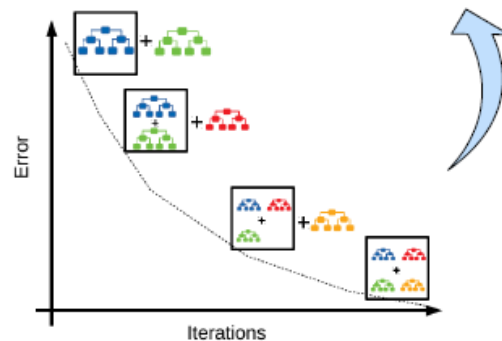
In the case of a limited number of data → simulations to train ML algorithm?



- External evaluation in 286 full PK profiles in kidney, heart and liver transplant recipients and comparison of predicted AUC_{0-12h} to that of the MAP Bayesian estimation based on the 0, 1 and 3h limited sampling strategy



- 9000 tacrolimus Monte Carlo simulations performed from a population pharmacokinetic model in mrgsolve
- Application of filters to remove unrealistic simulated profiles



<http://tvas.me/articles/2019/08/26/Block-Distributed-Gradient-Boosted-Trees.html>

Development of Xgboost machine learning algorithms :

- Splitting into a training (75%) and a test (25%) set subsets.
- Ten-fold cross-validation applied to the training set to tune the hyperparameters and evaluate the model performance

Pharmacological Research 167 (2021) 105578



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journal homepage: www.elsevier.com/locate/yphrs



Estimation of drug exposure by machine learning based on simulations from published pharmacokinetic models: The example of tacrolimus

Jean-Baptiste Woillard^{a,b,c,*}, Marc Labriffe^{a,b,c}, Aurélie Prémaud^{a,b}, Pierre Marquet^{a,b,c}

^a Univ. Limoges, IPPRIT, F-87000 Limoges, France

^b INSERM, IPPRIT, U1248, F-87000 Limoges, France

^c Department of Pharmacology and Toxicology, CHU Limoges, F-87000 Limoges, France



		Trained from simulations		Trained from ISBA*	
Organ transplanted	Method	Relative MPE (%)	relative RMSE (%)	Relative MPE (%)	relative RMSE (%)
kidney 1 (n = 137)	Xgboost 2 concentrations	1.08	8.5	-0.6	9.0
kidney 2 (n = 34)	Xgboost 2 concentrations	0.7	9.0	-1.0	9.1
liver (n = 68)	Xgboost 2 concentrations	5.9	12.9	3.3	12.9
heart (n = 47)	Xgboost 2 concentrations	3.2	11.4	-0.4	9.7



Paves the way / development of ML algorithms for TDM in different therapeutic areas / importance to validate on “real” data.

Ganciclovir in pediatrics: first dose prediction (PhD works L Ponthier)



Clinical Pharmacokinetics
<https://doi.org/10.1007/s40262-024-01362-7>

ORIGINAL RESEARCH ARTICLE

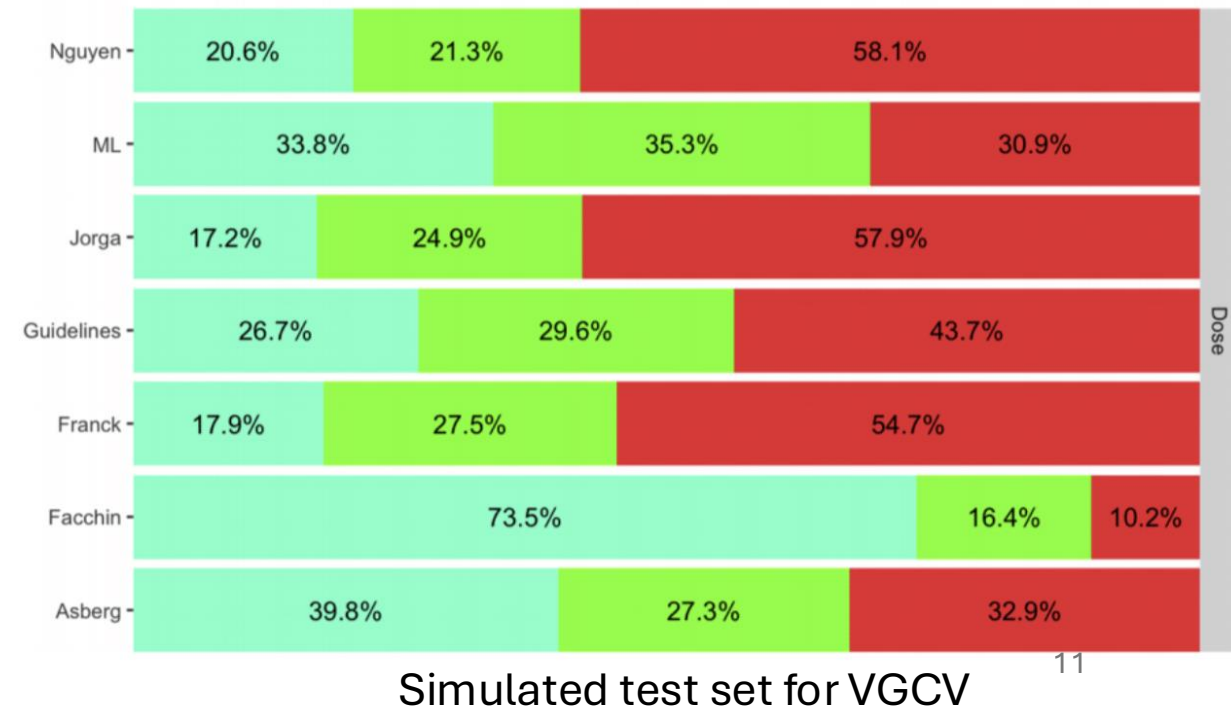


Optimization of Ganciclovir and Valganciclovir Starting Dose in Children by Machine Learning

Laure Ponthier^{1,2} · Julie Autmizguine^{3,4,5} · Benedicte Franck^{6,7} · Anders Åsberg^{8,9} · Philippe Ovetchkine⁴ · Alexandre Destere¹⁰ · Pierre Marquet^{1,11} · Marc Labriffe^{1,11} · Jean-Baptiste Woillard^{1,11}

- Monte Carlo simulations → 10800 patients from literature POPPK models (2 GCV IV, 3 GCV oral)
- Train of a classification ML model to predict AUC_{0-24h} at SS in the target (40-60 mg*h/L)
- Iterative search of the first dose that maximise the target attainment
- Comparison of theoretical target attainment after administration of the dose ML with POPPK literature formulae

Ponthier *et al.* ClinPK 2024



Rituximab in anti-PLA2R1 GEM

- Train of a classification ML model to predict underexposure at month-3
- Rationalization of features based on biological criteria

Association of Variables	Accuracy
Age + Gender + BSA	0.4559
Age + Gender + BSA + GFR on D0	0.5294
Age + Gender + BSA + GFR on D0 + CD19 on D0	0.5
Age + Gender + BSA + GFR on D0 + anti-PLA2R1 antibody titer on D0	0.5441
Age + Gender + BSA + GFR on D0 + anti-PLA2R1 antibody titer on D0 + weight	0.5417
Age + Gender + BSA + GFR on D0 + anti-PLA2R1 antibody titer on D0 + height	0.5441
Age + Gender + BSA + GFR on D0 + anti-PLA2R1 antibody titer on D0 + BMI	0.4559
Age + Gender + BSA + GFR on D0 + anti-PLA2R1 antibody titer on D0 + serum albumin on M0	0.6324
Age + Gender + BSA + anti-PLA2R1 antibody titer on D0 + serum albumin on D0	0.6471
Age + Gender + BSA + anti-PLA2R1 antibody titer on D0 + serum albumin on D0 + serum creatinine on D0	0.6618
Age + Gender + BSA + anti-PLA2R1 antibody titer on D0 + serum albumin on D0 + serum creatinine on D0 + use of angiotensin-converting enzyme inhibitors	0.6471
Age + Gender + BSA + anti-PLA2R1 antibody titer on D0 + serum albumin on D0 + serum creatinine on D0 + use of angiotensin II receptor blockers	0.6471
Age + Gender + BSA + anti-PLA2R1 antibody titer on D0 + serum albumin on D0 + serum creatinine on D0 + use of furosemide	0.6471
Age + Gender + BSA + anti-PLA2R1 antibody titer on D0 + serum albumin on D0 + serum creatinine on D0 + use of hydrochlorothiazide	0.6471
Age + Gender + BSA + anti-PLA2R1 antibody titer on D0 + serum albumin on D0 + serum creatinine on D0 + serum albumin on D15	0.72
Age + Gender + BSA + serum albumin on D0 + serum creatinine on D0 + serum albumin on D15 + serum creatinine on D15	0.72
Age + Gender + BSA + anti-PLA2R1 antibody titer on D0 + serum albumin on M0 + serum creatinine on D0 + serum albumin on D15 + serum creatinine on D15	0.794
Age + Gender + BSA + anti-PLA2R1 antibody titer on D0 + serum albumin on D0 + serum creatinine on D0 + serum albumin on D15 + serum creatinine on D15 + number of visits	0.748
Age + Gender + BSA + anti-PLA2R1 antibody titer on D0 + serum albumin on D0 + serum creatinine on D0 + serum albumin on D15 + serum creatinine on D15 + proteinuria on D0	0.7647
Age + Gender + BSA + anti-PLA2R1 antibody titer on D0 + serum albumin on D0 + serum creatinine on D0 + serum albumin on D15 + serum creatinine on D15 + proteinuria on D15	0.75
All predictors (N = 21)	0.7353

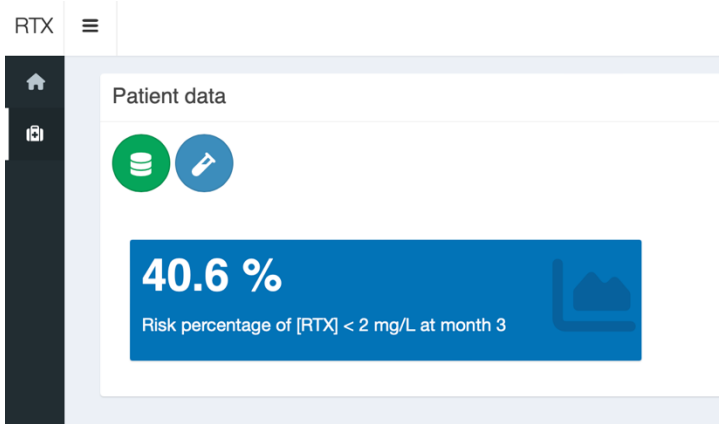
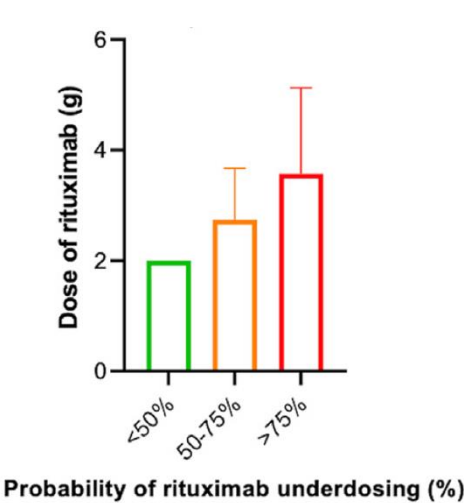
Performance Assessment Criteria	Training Data Set	Testing Data Set
Accuracy (%)	79.4	79.2
No information rate (%)	69.1	54.2
Sensitivity (%)	78.7	84.6
Specificity (%)	81.0	72.7
Positive predictive value (%)	90.2	78.6
Negative predictive value (%)	63.0	80.0
F-score (%)	84.1	81.5

Optimization of Rituximab Therapy in Adult Patients With PLA2R1-Associated Membranous Nephropathy With Artificial Intelligence



Alexandre Destere^{1,9,10}, Maxime Teisseyre^{2,3,4,10}, Diane Merino¹, Marion Cremonini^{3,5}, Alexandre O Gérard^{1,4}, Thomas Crepin⁶, Noémie Jourde-Chiche⁷, Daisy Graça^{2,3,5}, Kévin Zorzi^{2,3}, Céline Fernandez^{2,3}, Vesna Brglez^{2,3,5}, Sylvia Benzaken⁵, Vincent L.M. Esnault^{2,4}, Sylvain Benito⁸, Milou-Daniel Drici^{1,10} and Barbara Seitz-Polski^{2,3,4,5,10}

Destere *et al.* KIR 2023

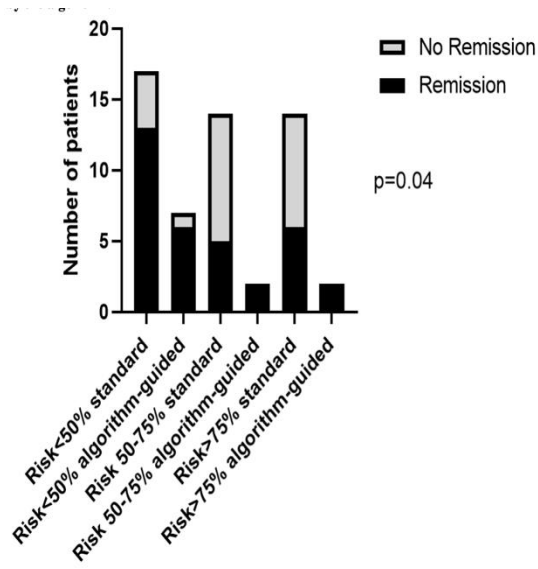


Rituximab in anti-PLA2R1 GEM (preliminary study of hospital clinical research program PHRC)

- Calculation of underexposure prediction and derivation of individualized dose
 - < 50 % : 1g x 2 (D0 and D15)
 - 50-75% : 1g x 3 (D0, D15 and M1)
 - > 75 % : 1g x 4 (D0, D15, M1 and M1.5)

• Reference : previous patient treated by RTX

- N = 11 patients
 - < 50 % : 7
 - 50-75% : 2
 - > 75 % : 2

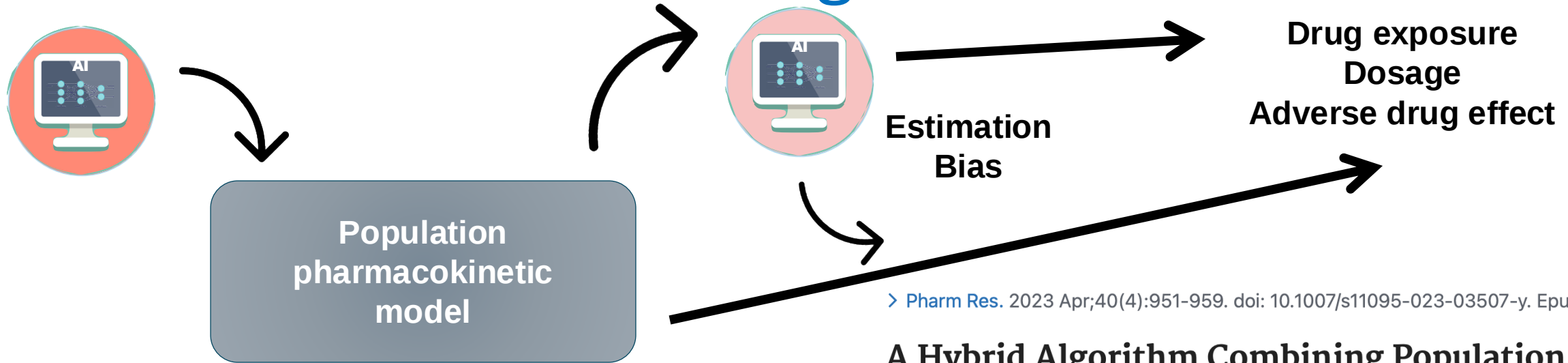


Artificial intelligence to guide rituximab therapy in patients with PLA2R1-associated membranous nephropathy

Maxime Teisseyre^{*1,2,3,4}, Alexandre Destere^{*5,6}, Marion Cremoni^{1,2,3,4}, Sonia Boyer-Suavet⁷, Alexandre Karamé⁸, Léa Corlu⁹, Gabrielle Duneau¹⁰, Kévin Zorzi^{1,3}, Céline Fernandez^{1,3}, Vesna Brglez^{1,3,4}, Sylvia Benzaken⁴, Guillaume Favre², Vincent L. M. Esnault^{1,2}, Sylvain Benito¹¹, and Barbara Seitz-Polski^{1,2,3,4}

Trials	n	Immunological remission*	Clinical remission
Algorithm-guided rituximab treatment	11	91 %	91%
GEMRITUX rituximab (23)	37	50%	35%
GEMRITUX NIAT (23)	38	12%	21%
RI-CYCLO rituximab (24)	37	63%	51%
RI-CYCLO cyclophosphamide-corticosteroid (24)	37	50%	65%
MENTOR rituximab (22)	65	52%	35%
MENTOR cyclosporin (22)	65	28%	49%
STARMEN tacrolimus-rituximab (32)	43	70%	44%
STARMEN cyclophosphamide-corticosteroid (32)	43	92%	74%
High-dose rituximab (15)	28	78%	64%

Use of Machine Learning in Pharmacometrics



> [Pharm Res.](#) 2023 Apr;40(4):951-959. doi: 10.1007/s11095-023-03507-y. Epub 2023 Mar 29.

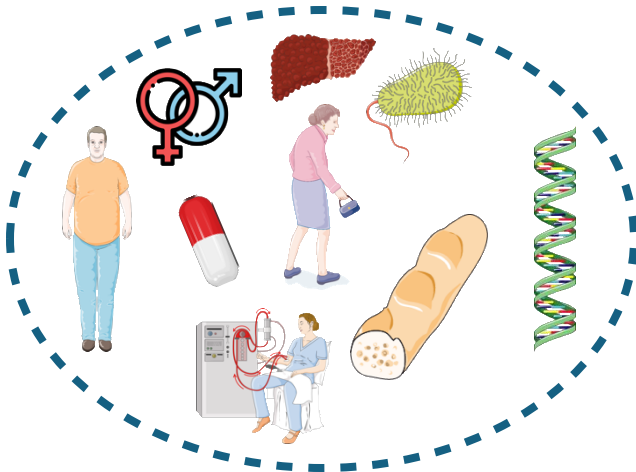
A Hybrid Algorithm Combining Population Pharmacokinetic and Machine Learning for Isavuconazole Exposure Prediction

Alexandre Destere ^{1 2}, Pierre Marquet ^{1 3}, Marc Labriffe ^{1 3}, Milou-Daniel Drici ², Jean-Baptiste Woillard ^{4 5}

> [Clin Pharmacokinet.](#) 2022 Aug;61(8):1157-1165. doi: 10.1007/s40262-022-01138-x. Epub 2022 May 31.

A Hybrid Model Associating Population Pharmacokinetics with Machine Learning: A Case Study with Iohexol Clearance Estimation

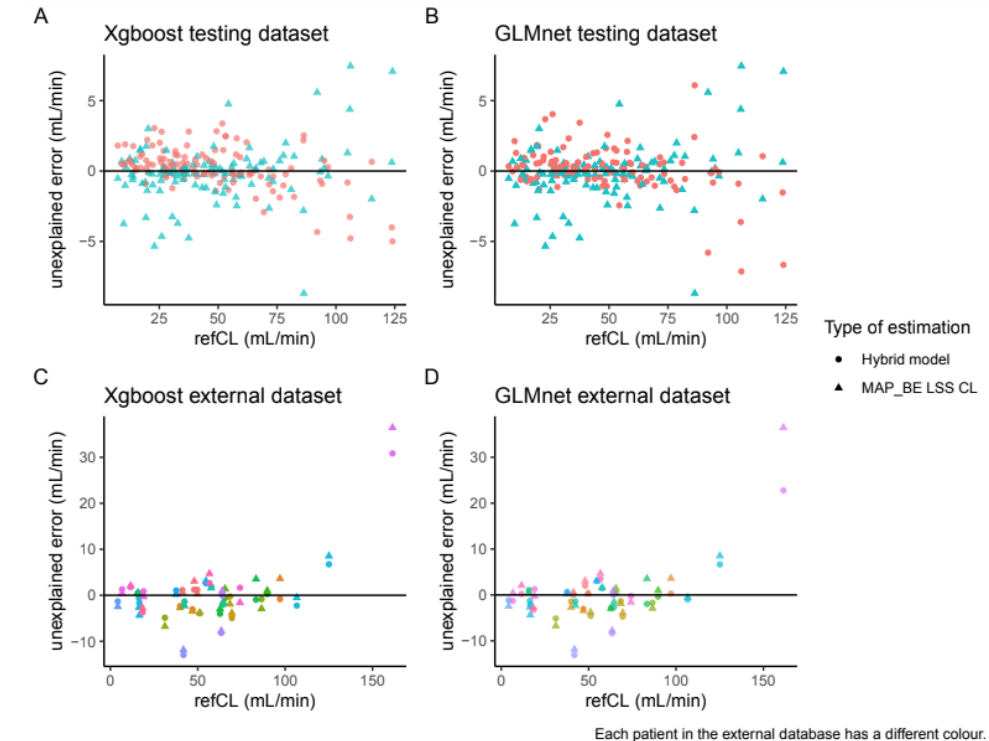
Alexandre Destere ^{1 2 3}, Pierre Marquet ^{1 2}, Charlotte Salmon Gandonnière ⁴, Anders Åsberg ^{5 6}, Véronique Loustaud-Ratti ^{1 7}, Paul Carrier ⁷, Stephan Ehrmann ^{4 8}, Chantal Barin-Le Guellec ¹, Aurélie Premaud ¹, Jean-Baptiste Woillard ^{9 10}



Hybrid model: combination of ML and POPPK to keep interpretability:

iohexol (PhD works A Destere) (1)

- Simulation of 500 patients / iohexol for estimation of iohexol CL (GFR) from a literature POPPK model (2)
- MAP-BE on simulations
 - All samples (REF)
 - 3 samples (LSS)
 - Calculation of residual error (REF – LSS)
- Train ML algorithm to learn residual error (**from data obtained by MAP-BE**: observed concentrations, PK parameters + featured engineering eg diff between observed concentrations)
- Evaluation in the train (10-fold CV), test and external real data



1-Destere A et al. A Hybrid Model Associating Population Pharmacokinetics with Machine Learning: A Case Study with Iohexol Clearance Estimation. *Clin Pharmacokinet.* 2022

2-Destere A et al. A single Bayesian estimator for iohexol clearance estimation in ICU, liver failure and renal transplant patients. *Br J Clin Pharmacol.* 2022;88:2793–801.

Hybrid model: combination of ML and POPPK to keep interpretability:

iohexol (PhD works A Destere) (1)

	Training		Testing		External	
	MAP-BE LSS	Hybrid model Xgboost	MAP-BE LSS	Hybrid model Xgboost	MAP-BE LSS	Hybrid model Xgboost
MPE%	-2.0	-0.3	-1.0	0.7	-3.7	-2.2
RMSE%	10.1	7.5	6.2	5.7	14.3	10.9
MPE out of $\pm 20\%$ (%)	4.0	2.8	1.7	0.9	13.9	8.3

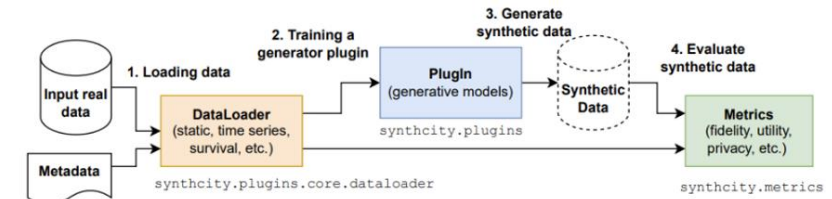
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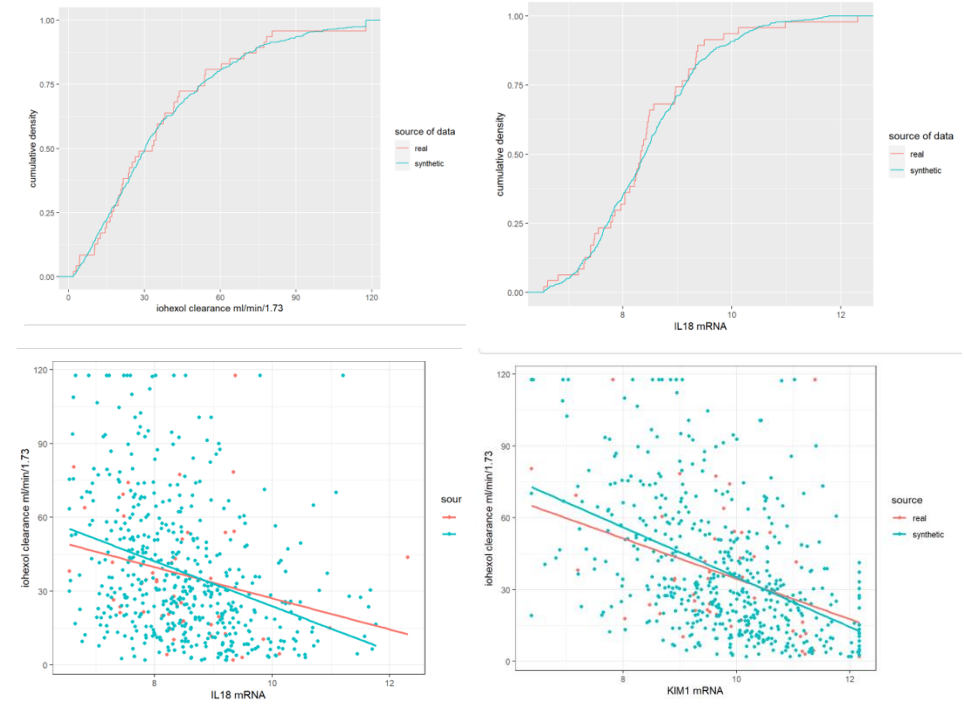
Creation of synthetic patients by ML/DL



- Creation of virtual patients: continuous or categorical variables regardless of their distribution (e.g., GAN)
- Balance between **utility and privacy**
- Improvement of predictive model performances (limited data = often the case in Pharmacometrics)
- Alternative to federated learning: creation of virtual data twin of local data → **sharing between centers** (useful for multicentric projects)



Qian et al. 2023 <https://arxiv.org/abs/2301.07573>



Recent synthetic data approach privacy validated by CNIL (French National commission for informatics & privacy)

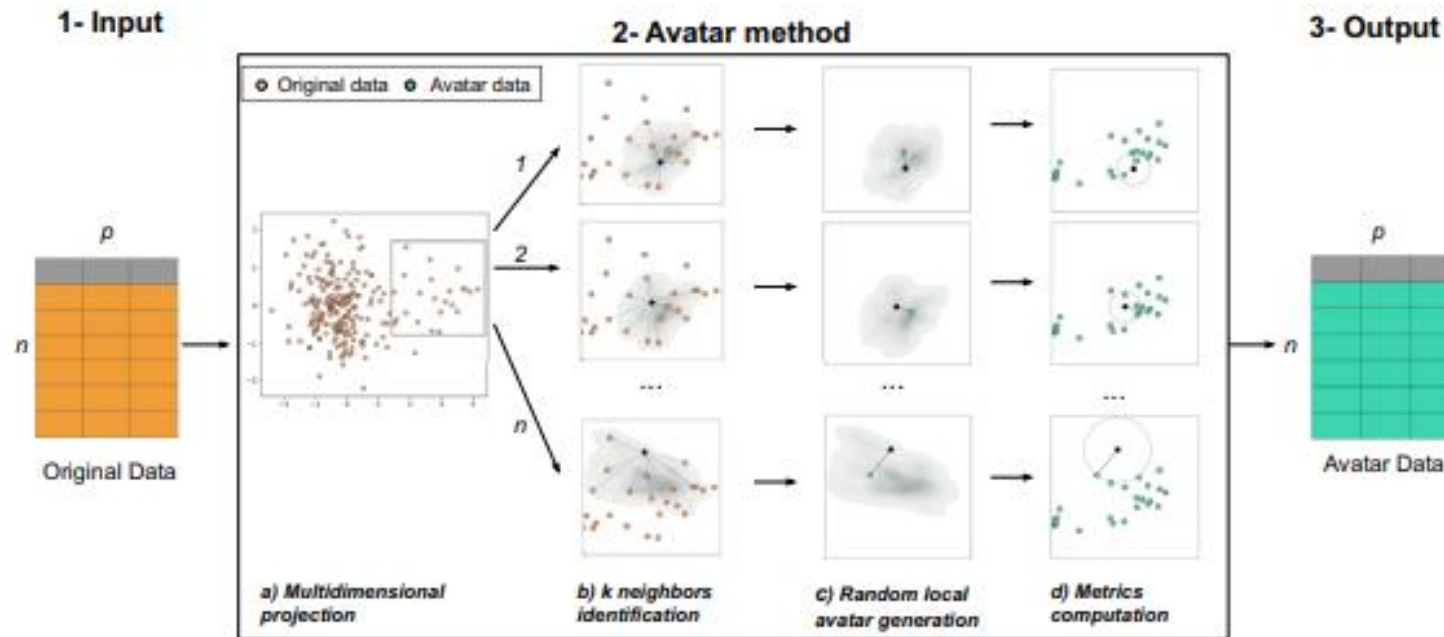
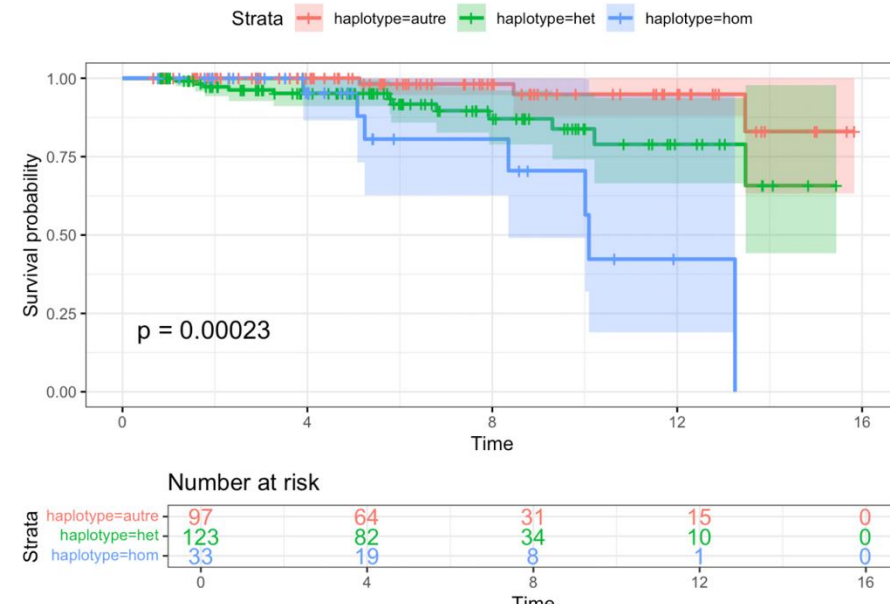


Fig. 5 The Avatar method uses local modeling to stochastically generate a synthetic individual, termed an avatar simulation. (1) Original pseudonymized sensitive data. **(2)** The core of the Avatar method consists of four steps: (a) individuals are projected in a multidimensional space; (b) pairwise distances are computed to find the k nearest neighbors (here $k = 12$) in a reduced space; (c) a synthetic individual is pseudo-randomly generated in the subspace defined by the neighbors; (d) privacy metrics are evaluated. **(3)** Output of the dataset of synthetic data. More details are provided online (<https://docs.octopize.io/>).

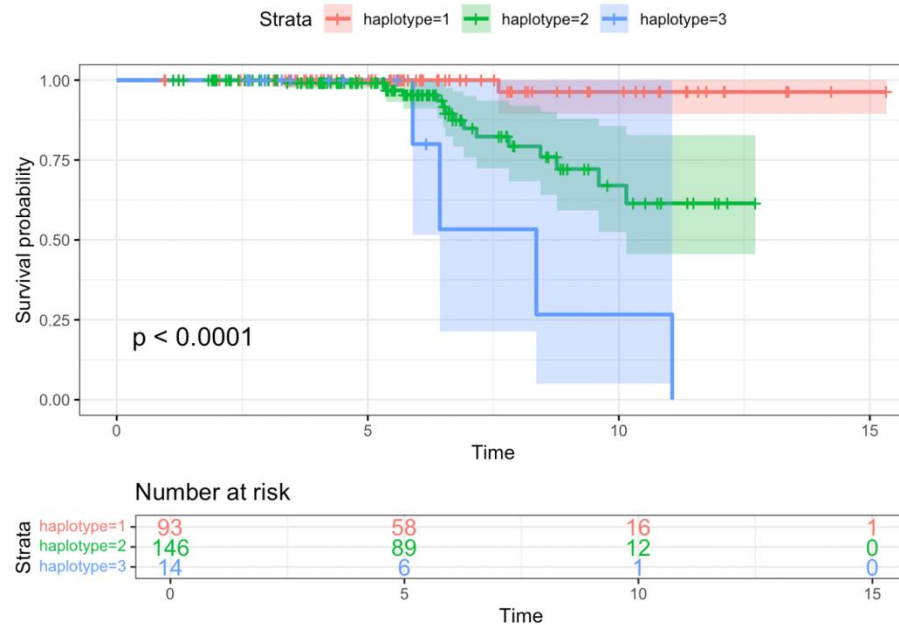
Guillaudeau et al Nature Digital Med 2023 *Patient-centric synthetic data generation, no reason to risk reidentification in biomedical data analysis*

Benchmarking of different approaches

Original data



Avatar k=10



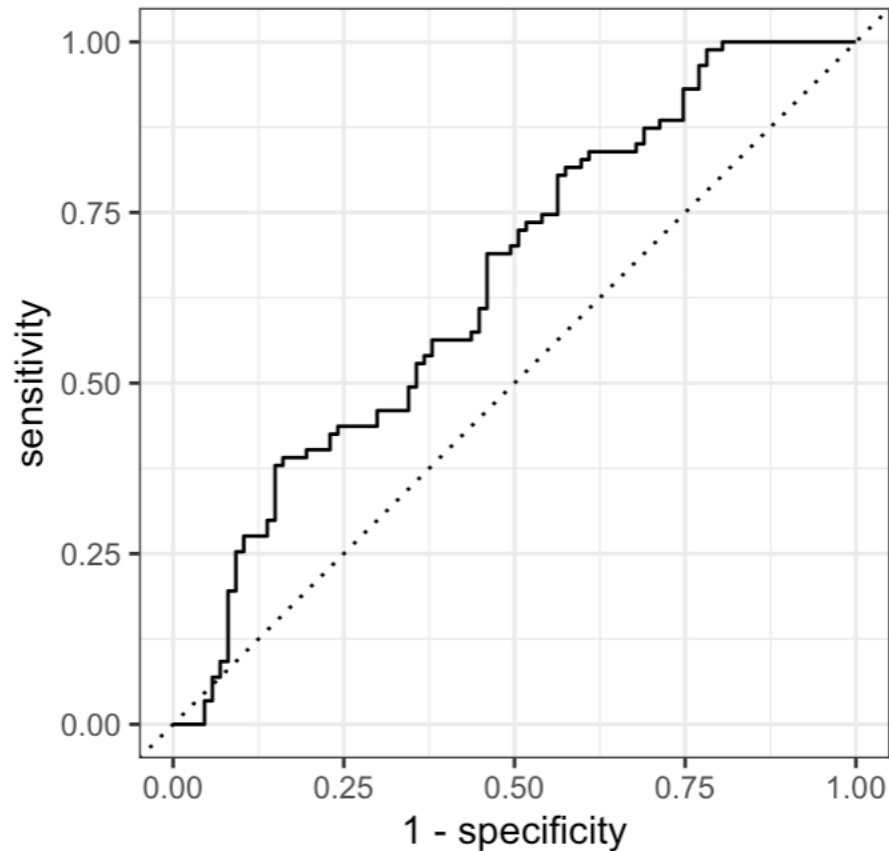
Algorithm	KL inverse	KS test	DCR* [5th-50th-95th]	NNDR* [5th-50th-95th]	AUC ROC#
Original data	NA	NA	NA	NA	NA
Avatar k=5	0.87	0.72	[0.28-0.57-1.00]	[0.14-0.33-0.75]	0.581
Avatar k=5 augmented	0.93	0.92	[0.09-0.42-1.51]	[0.05-0.27-0.94]	0.534
Avatar K k=10	0.79	0.90	[0.50-1.00-2.14]	[0.34-0.72-0.97]	0.550
Avatar k=10 augmented	0.89	0.91	[0.19-0.68-1.51]	[0.10-0.47-0.94]	0.518
Avatar k=20	0.77	0.89	[0.47-1.04-1.90]	[0.34-0.74-0.98]	0.503
Avatar k=20 augmented	0.76	0.88	[0.47,1.01,1.87]	[0.32-0.74-0.94]	0.474
CT-GAN	0.78	0.88	[0.83-1.78-3.39]	[0.52-0.87-0.99]	0.234
CT-GAN augmented	0.89	0.91	[0.81-1.87-3.62]	[0.52-0.87-0.99]	0.345
surVAE	0.84	0.89	[0.89-1.01-2.99]	[0.55-0.88-0.99]	0.298
surVAE augmented	0.86	0.90	[0.86-1.94-3.08]	[0.54-0.90-0.99]	0.367

Synthetic data in POPPK

Can synthetic data be the key to overcoming data sharing in pharmacometrics? A case study of tacrolimus in heart transplant patients

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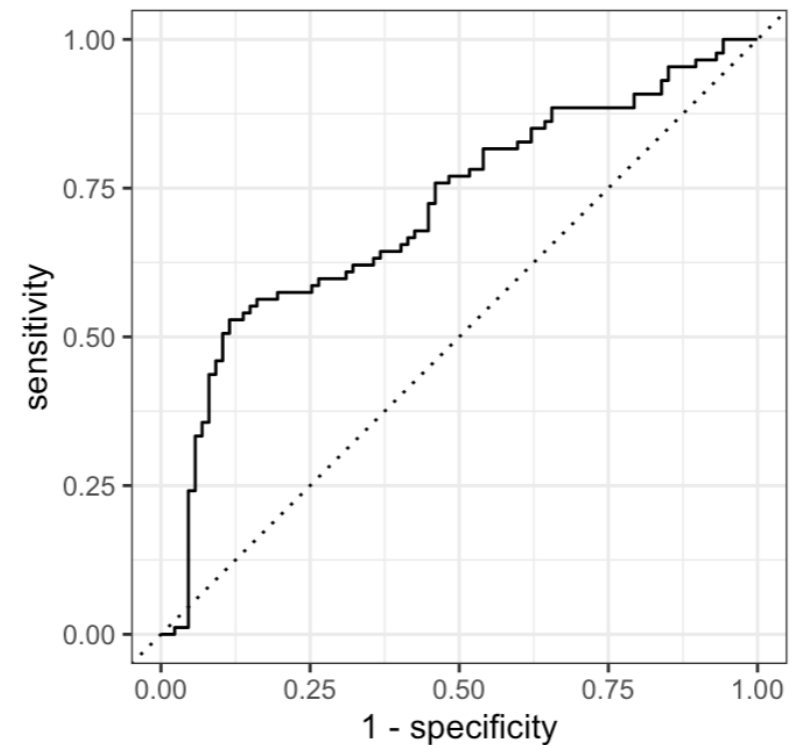
Under review CPT: PS



Avatar with K = 5

→ Evaluate the no-tracability of real data

→ Logistic regression to determine real or synthetic data



Avatar with K = 15

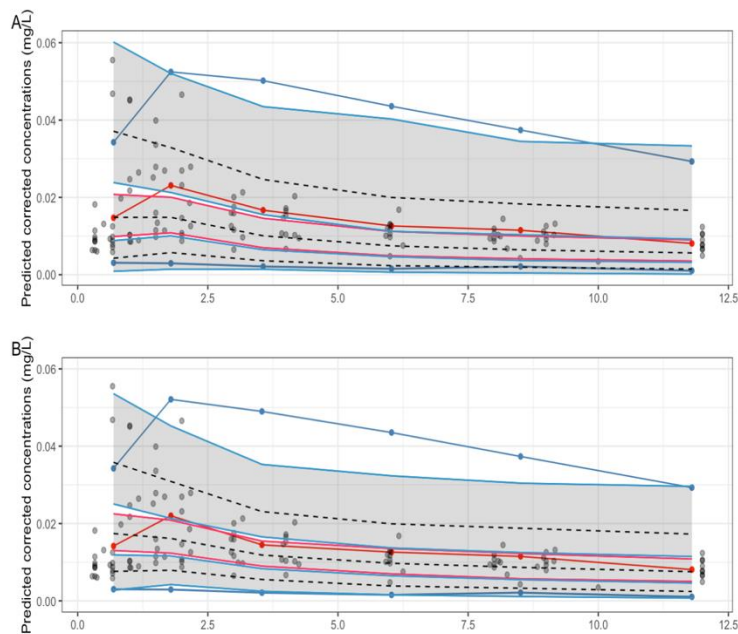
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Under review CPT: PS

- Evaluate the abilities of tabular generative algorithms to create synthetic PK to develop POPPK model
- Focus on structural model



> Br J Clin Pharmacol. 2023 Dec;89(12):3584-3595. doi: 10.1111/bcp.15857. Epub 2023 Aug 10.

Tacrolimus population pharmacokinetics in adult heart transplant patients

	Paschier et al. Original development dataset	k=5	k=5 augmented	k=15	k=15 augmented	CTGAN	CTGAN augmented	TVAE	TVAE augmented
Best model	2cp ~ TrCp	2cp ~ TrCp	2cp ~ Tlag	2cp ~ TrCp	2cp ~ Tlag	2cp ~ Tlag	2cp ~ Tlag	2cp ~ TrCp	2cp ~ Tlag
Tlag (RSE%)	-	-	0.3 (3.3)	-	0.3 (0.7)	0.3 (14.4)	0.4 (6.9)	-	0.3 (6.0)
Ktr (RSE%)	4.74 (Fixed)	8.7 (19.1)	-	23.8 (NE)	-	-	-	7.1 (13.8)	-
Mtt (RSE%)	0.5 (11.4)	0.4 (8.17)	-	0.3 (54.2)	-	-	-	0.6 (6.8)	-
Ka (RSE%)	1.0 (8.4)	0.6 (7.7)	0.7 (3.2)	13.7 (67.7)	8.5 (6.3)	0.6 (6.5)	0.4 (6.6)	1.2 (22.6)	0.9 (7.0)
CI (RSE%)	15.5 (10.9)	14.6 (8.7)	14.7 (4.6)	10.4 (NE)	0.2 (30.1)	14.7 (14.3)	14.7 (6.9)	11.5 (10.1)	10.2 (6.0)
V1 (RSE%)	21.2 (34.4)	10.5 (21.1)	23.8 (7.3)	146 (46.2)	175 (2.8)	29.4 (18.2)	19.2 (10.6)	0.0008 (NE)	27 (12.9)
Q (RSE%)	78.3 (11.2)	68.4 (8.4)	66.3 (4.8)	39.7 (97.3)	49.9 (5.2)	47.8 (21.1)	43.8 (8.8)	109 (16.7)	85.2 (6.7)
V2 (RSE%)	498.8 (16.7)	443 (15.5)	403 (6.4)	240 (NE)	2140 (3.5)	340 (54.7)	378 (13.2)	375 (17.8)	368 (9.9)
ωTlag (RSE%)	-	-	0.3 (12.6)	-	0.05 (13.5)	0.5 (19.1)	0.5 (9.0)	-	0.5 (10.1)
ωKtr (RSE%)	-	0.6 (26.6)	-	0.6 (105)	-	-	-	0.1 (109)	-
ωMtt (RSE%)	0.6 (16.0)	0.2 (31.7)	-	0.2 (135)	-	-	-	0.03 (143)	-
ωKa (RSE%)	0.2 (49.7)	0.2 (40.4)	0.2 (11.8)	0.8 (20.7)	0.5 (8.7)	0.1 (119.0)	0.2 (20.4)	0.3 (52.7)	0.2 3(23.5)
ωCI (RSE%)	0.7 (12.7)	0.4 (15.4)	0.5 (7.1)	0.6 (47.1)	0.7 (34.1)	0.6 (47.0)	0.6 (8.5)	0.4 (16.3)	0.5 (7.8)
ωV1 (RSE%)	2.5 (17.6)	0.3 (98.2)	0.6 (11.1)	0.2 (60.6)	0.3 (6.9)	0.2 (49.5)	0.3 (36.0)	3.2 (96.5)	0.4 (15.9)
ωQ (RSE%)	0.6 (16.4)	0.3 (17.8)	0.4 (8.2)	0.5 (78.4)	0.5 (7.0)	0.7 (18.4)	0.5 (12.0)	0.5 (17.7)	0.6 (9.8)
ωV2 (RSE%)	1.0 (16.2)	0.7 (17.5)	0.6 (8.3)	1.1 (69.9)	0.4 (7.8)	0.5 (208)	0.8 (13.2)	0.8 (17.3)	0.9 (7.8)
a (mg/L)	-	-	-	-	-	-	-	-	-
b (%)	0.12 (4.3)	0.06 (5.8)	0.07 (2.7)	0.05 (9.3)	0.06 (2.6)	0.22 (6.5)	0.23 (2.6)	0.13 (5.4)	0.14 (2.6)



Thanks !

